

Compare Newton's method with fixed point iteration.

Rewrite  $(x-2)^2 - \ln x = 0$  as a fixed point problem

A)  $(x-2)^2 = \ln x \rightarrow x = e^{(x-2)^2}$

$$|g'(x)| < |g'(1)| \leq 2e$$

$n$	$g(p_n)$
0	1.5
1	1.284025417
2	1.669659317
3	1.115301717
4	2.187350626

← Diverges

$n$	$g(p_n)$
0	2
1	2.8325546
2	3.0203817

3)  $x-2 = \sqrt{\ln x}$   
 $x = 2 + \sqrt{\ln x}$

bad because  $g'(x)$  is unbounded at  $x=1$

c)  $x^2 - 4x + 4 = \ln x$   
 $x = \frac{x^2 - \ln x + 4}{4}$

$g(x) = \frac{x^2 - \ln x + 4}{4}$  — increasing

$g(1) \leq g(x) \leq g(2)$   
 $1 < \frac{5}{4} \leq g(x) \leq 2 - \frac{\ln 2}{4} <$

$$g'(x) = \frac{2x - \frac{1}{x}}{4} = \frac{x}{2} - \frac{1}{4x}$$