

Determining  $a_0$  is easy

$$a_0 = P_n(x_0) = f_0 := f(x_0)$$

To determine  $a_1$  we have

$$P_n(x_1) = a_0 + a_1(x_1 - x_0)$$

$$f_1 = f_0 + a_1(x_1 - x_0)$$

$$\Rightarrow a_1 = \frac{f_1 - f_0}{x_1 - x_0}$$

Def: The zeroth divided difference of the function  $f$  with respect to  $x_i$  is denoted by  $f[x_i]$  and is defined as

$$f[x_i] = f(x_i)$$

The remaining divided differences are defined inductively

Def: The first divided difference of  $f$  with respect to  $x_i, x_{i+1}$  is denoted by  $f[x_i, x_{i+1}]$  and is defined as follows

$$f[x_i, x_{i+1}] = \frac{f[x_{i+1}] - f[x_i]}{x_{i+1} - x_i}$$