

The errors of the interpolation are

Degree	$P_n(1.75)$	Actual Error	$\max f^{(n+1)} $	Error Bound	Next-to rule
1	1.25665	0.01995	0.3679	0.03725	0.0285
2	1.2852	-0.0086			
3	1.2861	-0.0095			

Typically we can expect that a higher degree polynomial will approximate better. But in this case the approximation of the degree 3 polynomial is worse than that of degree 2 polynomial.

$$E_1(x, f) = \frac{f''(\xi)}{2!} (x-1.1)(x-2)$$

$$f'(x) = 2xe^{-\frac{x}{2}} - x^2 \cdot \frac{1}{2} e^{-\frac{x}{2}} = \left(2x - \frac{x^2}{2}\right) e^{-\frac{x}{2}}$$

$$f''(x) = (2-x)e^{-\frac{x}{2}} - \frac{1}{2} \left(2x - \frac{x^2}{2}\right) e^{-\frac{x}{2}} =$$

$$= \left(2-x-x+\frac{x^2}{4}\right) e^{-\frac{x}{2}} = \left(2-2x+\frac{x^2}{4}\right) e^{-\frac{x}{2}}$$

$$f'''(x) = \left(-2+\frac{x}{2}\right) e^{-\frac{x}{2}} - \frac{1}{2} \left(2-2x+\frac{x^2}{4}\right) e^{-\frac{x}{2}}$$

$$= \left(-3+\frac{3}{2}x-\frac{x^2}{8}\right) e^{-\frac{x}{2}} = 0$$